ABSTRACT. It is natural to ask whether one can extend the notion of a Haar subspace so as to be valid in an *arbitrary* normed linear space, and at the same time preserve as much of the $C[a, b]$-theory as possible. In this paper we introduce the notion of an *interpolating subspace* of a normed linear space. In the particular space $C(T)$, T compact Hausdorff, the interpolating subspaces turn out to be precisely the Haar subspaces. (Recall that an n-dimensional subspace M of $C(T)$ is called a *Haar subspace* if every function in $M \setminus \{0\}$ has at most $n - 1$ zeros in T.) We shall verify that *corresponding to each one of the classical results which hold for Haar subspaces in* $C[a, b]$, *there is a strictly analogous result valid for interpolating subspaces in an arbitrary normed linear space.*