ABSTRACT. We consider a general problem of best approximation in Hilbert space by a set which is the intersection of a convex cone and a linear variety. This includes the well-known problem of "shape-preserving" interpolation as a special case. We examine the particular case when the cone is the set of N-convex functions.