ABSTRACT. A generating basis and the dual cone of n-convex functions satisfying certain constraints are derived. As applications, the existence and characterization of a best L_p-approximation ($1 \leq p < \infty$) from such subcones to a function in L_p are established. The relationship between a best L_1-approximation and perfect splines is developed under certain conditions.