ABSTRACT. A generating basis and the dual cone of $n$-convex functions satisfying certain constraints are derived. As applications, the existence and characterization of a best $L_p$-approximation ($1 \leq p < \infty$) from such subcones to a function in $L_p$ are established. The relationship between a best $L_1$-approximation and perfect splines is developed under certain conditions.