ABSTRACT. Let C be a closed convex subset of the Hilbert space H, A a bounded linear operator from H to a finite-dimensional Hilbert space Y, $b \in Y$, and $K(b) = C \cap A^{-1}(b)$. A survey is given of recent results concerned mainly with characterizing and computing best approximations of elements x in H from the set $K(b)$.